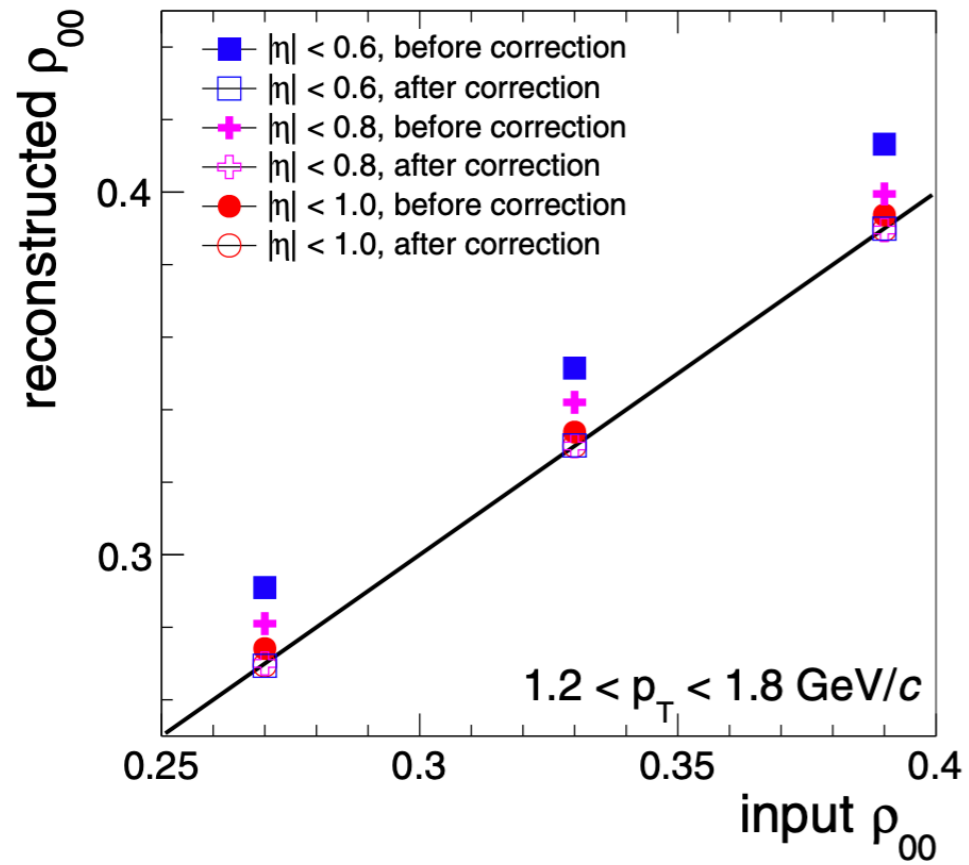
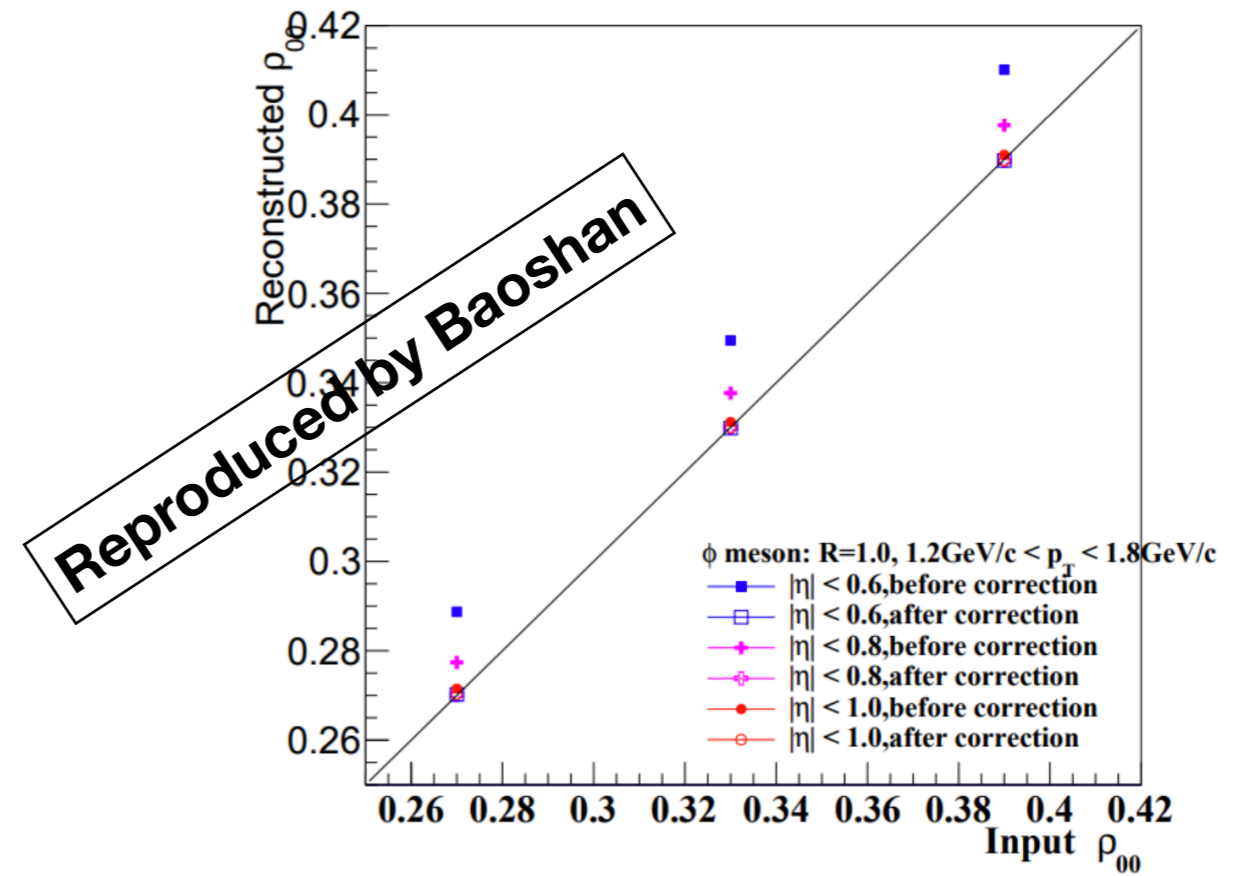


**Summary on April 7, 2023 - nonzero  $\langle \cos^2\beta \rangle$  in a small eta cut**

**Diyu Shen**

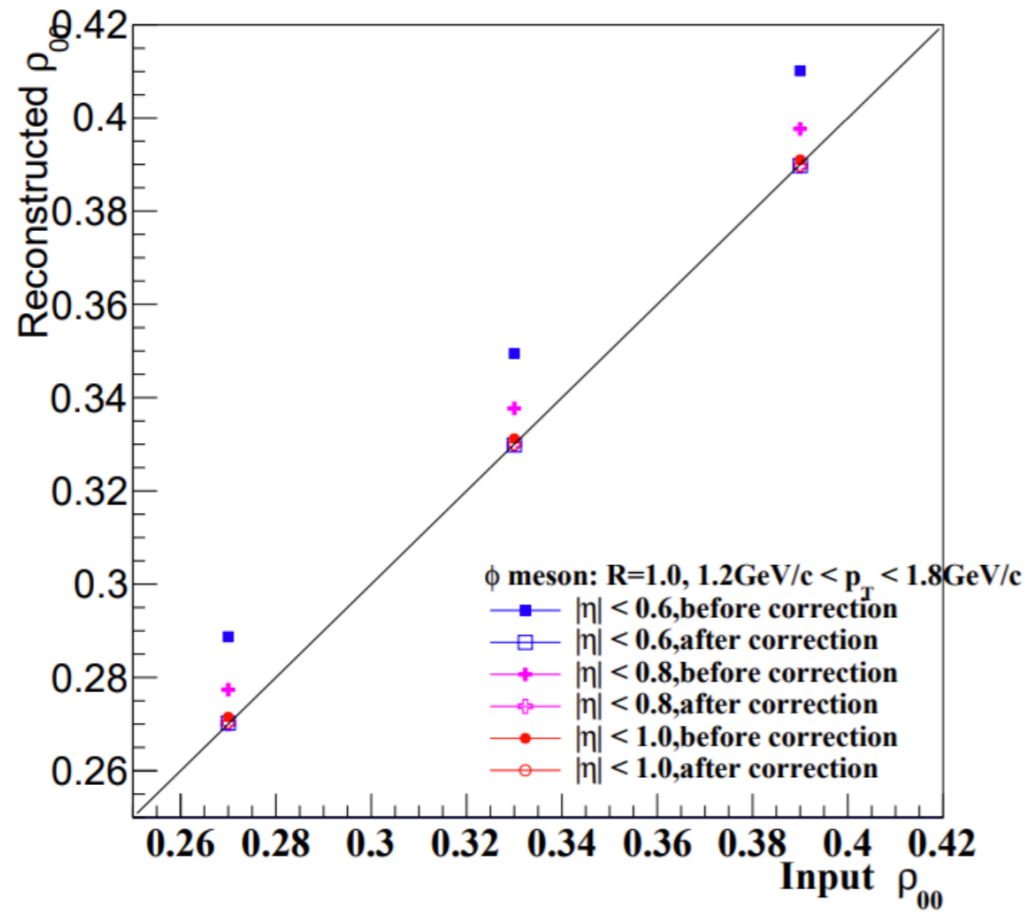


R=1

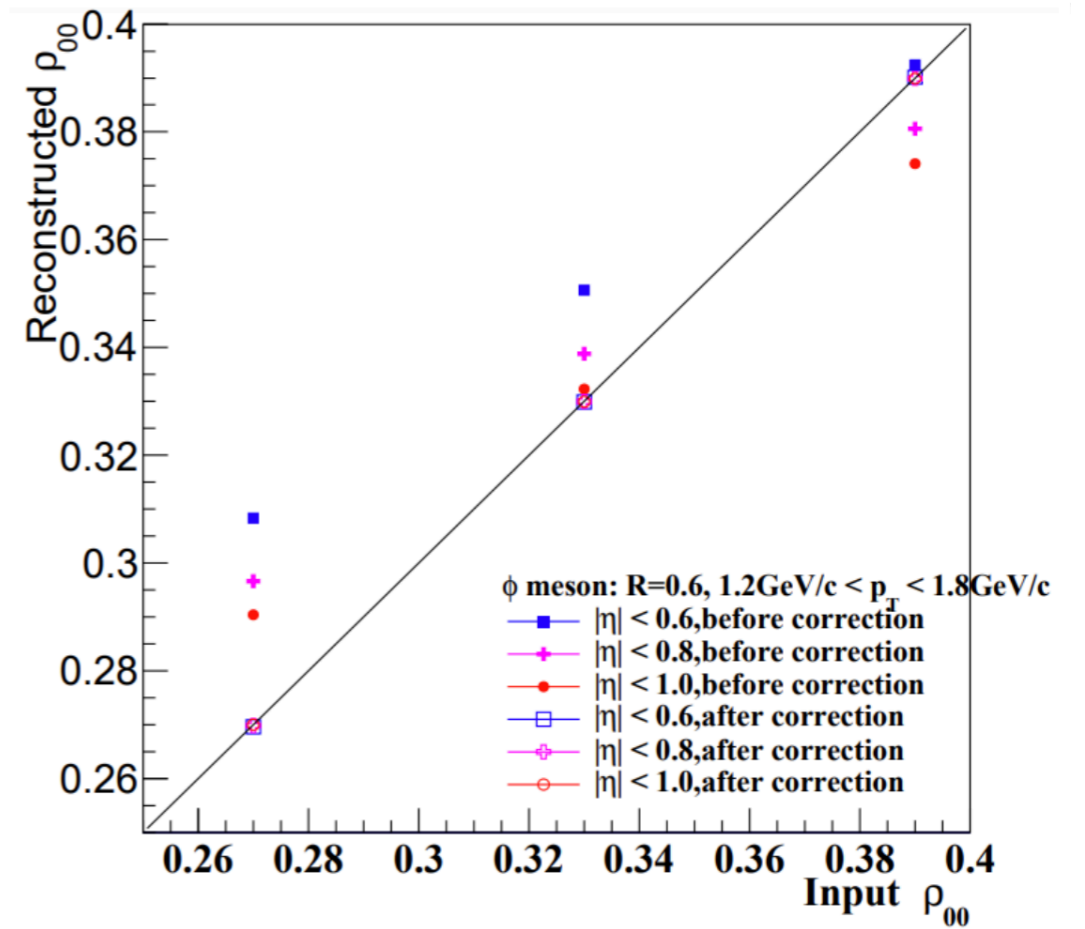


This plot is obtained by using reaction plane, i.e. resolution = 1.

R=1



R=0.6



For finite event plane resolution, observed  $\rho_{00}$  is “rotated”, but still can be corrected to the input.

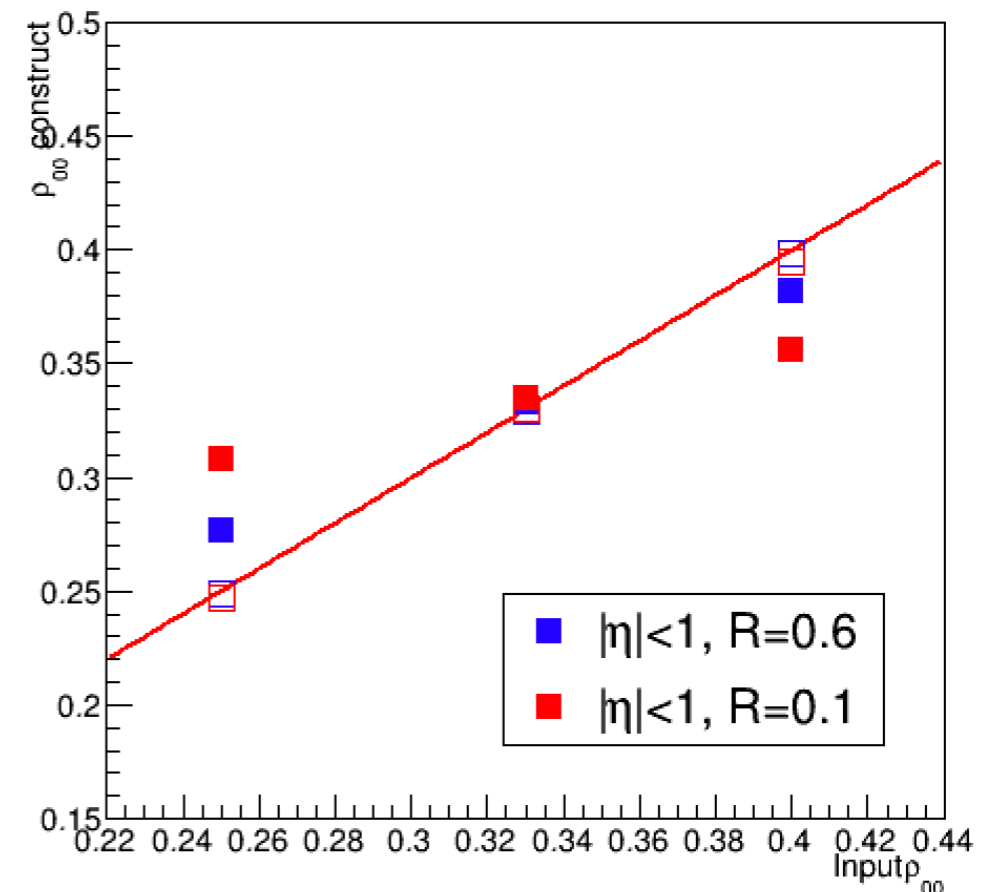
## Dependence of the extracted F on the $\rho_{00}$ and resolution:

$$g(\theta^*, \beta) = 1 + F^* \cos^2 \theta$$
$$\propto 1 + F \cos^2 \theta^* + F \sin^2 \theta^* \cos 2\beta, \quad (23)$$

As eq. 23 is an approximation of acceptance effect, and it is obtained by fitting  $\cos(\theta^*)$  distribution with  $\propto 1 + F \cos^2 \theta^*$  which requires  $\langle \cos 2\beta \rangle = 0$ . It is not perfect so that F may have few percentage variation, but this has negligible effect on  $\rho_{00}$ .

In order to illustrate the effect, we simulated few cases:

1.  $|\eta| < 1$ , resolution = 1.0, input  $\rho_{00} = 0.25$
2.  $|\eta| < 1$ , resolution = 1.0, input  $\rho_{00} = 0.33$
3.  $|\eta| < 1$ , resolution = 1.0, input  $\rho_{00} = 0.40$
4.  $|\eta| < 1$ , resolution = 0.6, input  $\rho_{00} = 0.25$
5.  $|\eta| < 1$ , resolution = 0.6, input  $\rho_{00} = 0.33$
6.  $|\eta| < 1$ , resolution = 0.6, input  $\rho_{00} = 0.40$
7.  $|\eta| < 1$ , resolution = 0.1, input  $\rho_{00} = 0.25$
8.  $|\eta| < 1$ , resolution = 0.1, input  $\rho_{00} = 0.33$
9.  $|\eta| < 1$ , resolution = 0.1, input  $\rho_{00} = 0.40$



We use F obtained from  $|\eta| < 1$ , resolution = 1.0 (reaction plane), input  $\rho_{00} = 1/3$  to correct all those cases.

## Subtleties in coding:

There are two versions of the code, one is fitting  $\cos \theta^*$  histogram after eta cut directly with  $\propto 1 + F \cos^2 \theta^*$  function. In this version, the  $\cos \theta^*$  histogram is obtained **before** the spin alignment sampling introduced.

```
if(TMATH::Abs(KplusEta)<=eta_gap && TMATH::Abs(KminusEta)<=eta_gap){  
  h_theta->Fill(TMATH::Abs(CosThetaStarZP));  
  h_theta_star->Fill(TMATH::Abs(CosThetaStarSP));  
  CosBeta->Fill(0.5,cos(2.*beta));  
}  
  
if(!Sampling(f_rhoPhy,CosThetaStarRP)) return;  
  
if(TMATH::Abs(KplusEta)<=eta_gap && TMATH::Abs(KminusEta)<=eta_gap){  
  h_eta->Fill(TMATH::Abs(CosThetaStarSP));  
}  
  
return;
```

It is important to have **this distribution** to be a constant, so that g function is reflected by  $\cos \theta^*$  histogram after cut

$$\left[ \frac{dN}{d \cos \theta^* d\beta} \right]_{|\eta|} = \frac{dN}{d \cos \theta^* d\beta} \times g(\theta^*, \beta). \quad (22)$$

**Constant means  $\rho_{00} = 1/3$**

Another method fills  $\cos \theta^*$  histogram after the spin alignment sampling, in this case one has to take the ratio of  $\cos \theta^*$  histogram of before and after eta cut, then fits with  $\propto 1 + F \cos^2 \theta^*$

```

// Fill cos theta star EP after eta cut
if(!Sampling(f_rhoPhy, CosThetaStarRP)) return;
h_theta_star_before->Fill(TMath::Abs(CosThetaStarEP));

double eta_gap = 0.8;
double pt_gap = 0.2;
if(TMath::Abs(PiplusEta)<=eta_gap && TMath::Abs(PiminusEta)<=eta_gap) h_theta_star->Fill(TMath::Abs(CosThetaStarEP));
return;

```

$$\frac{\left[ \frac{dN}{d \cos \theta^* d\beta} \right]_{|\eta|}}{\frac{dN}{d \cos \theta^* d\beta}} = \frac{\cancel{dN}}{d \cos \theta^* d\beta} \times g(\theta^*, \beta). \quad (22)$$

```
h_theta_star->Divide(h_theta_star_before);
```

$$g(\theta^*, \beta) = 1 + F^* \cos^2 \theta$$

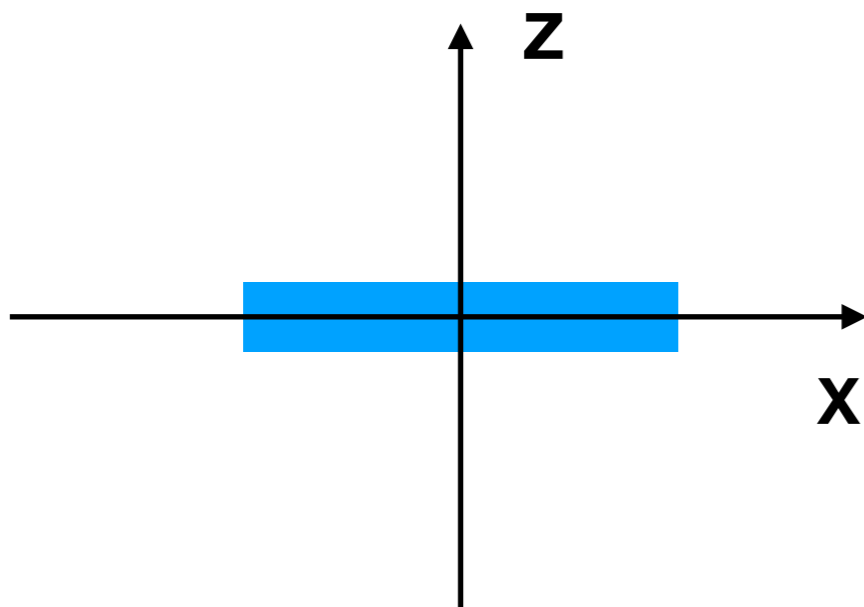
$$\propto 1 + F \cos^2 \theta^* + F \sin^2 \theta^* \cos 2\beta, \quad (23)$$

what has been used in the code:  $1 + F \cos^2 \theta^*$ , based on naive expectation  $\int \cos 2\beta d\beta = 0$

```
h_theta_star->Fit(Func_A, "ER");
```

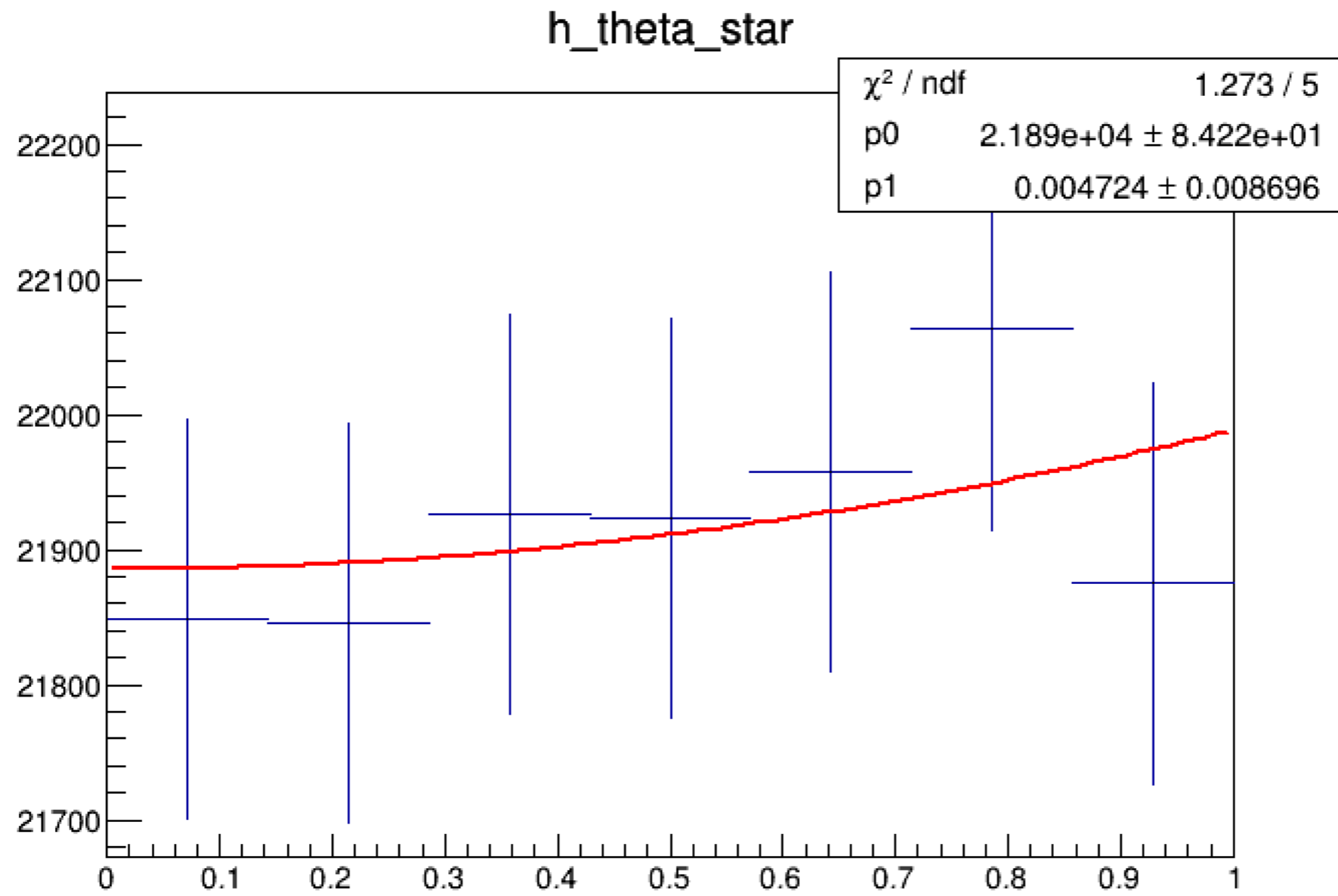
```
TF1 *Func_A = new TF1("Func_A", "[0]*(1.+[1]*(x*x))", 0, 1);
```

But this is only true for perfect acceptance, for finite acceptance " $v_2$ "  $\neq 0$



$$|\eta| < 1$$

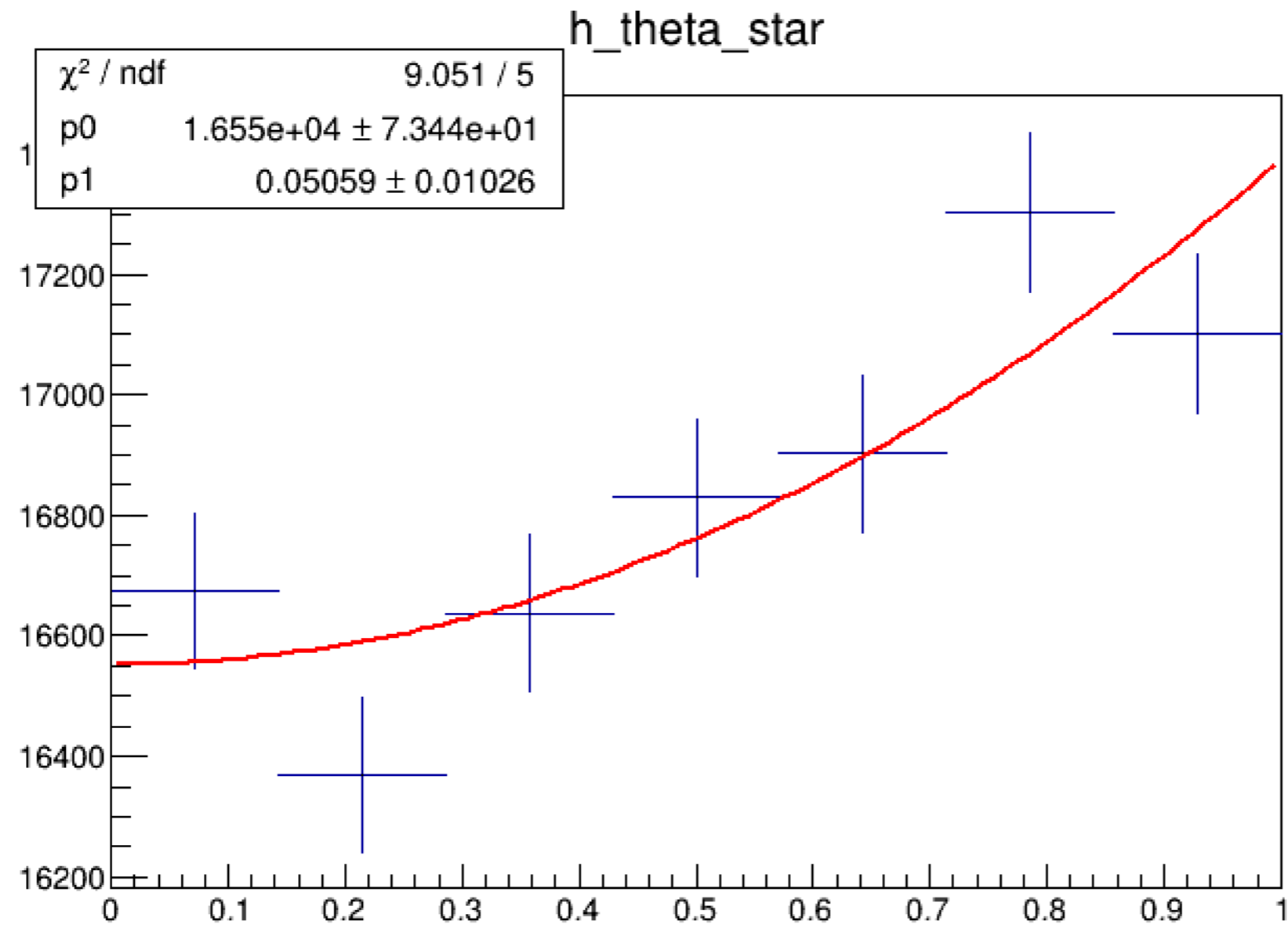
$$\cos 2\beta: 0.00207089 \pm 0.00180267$$





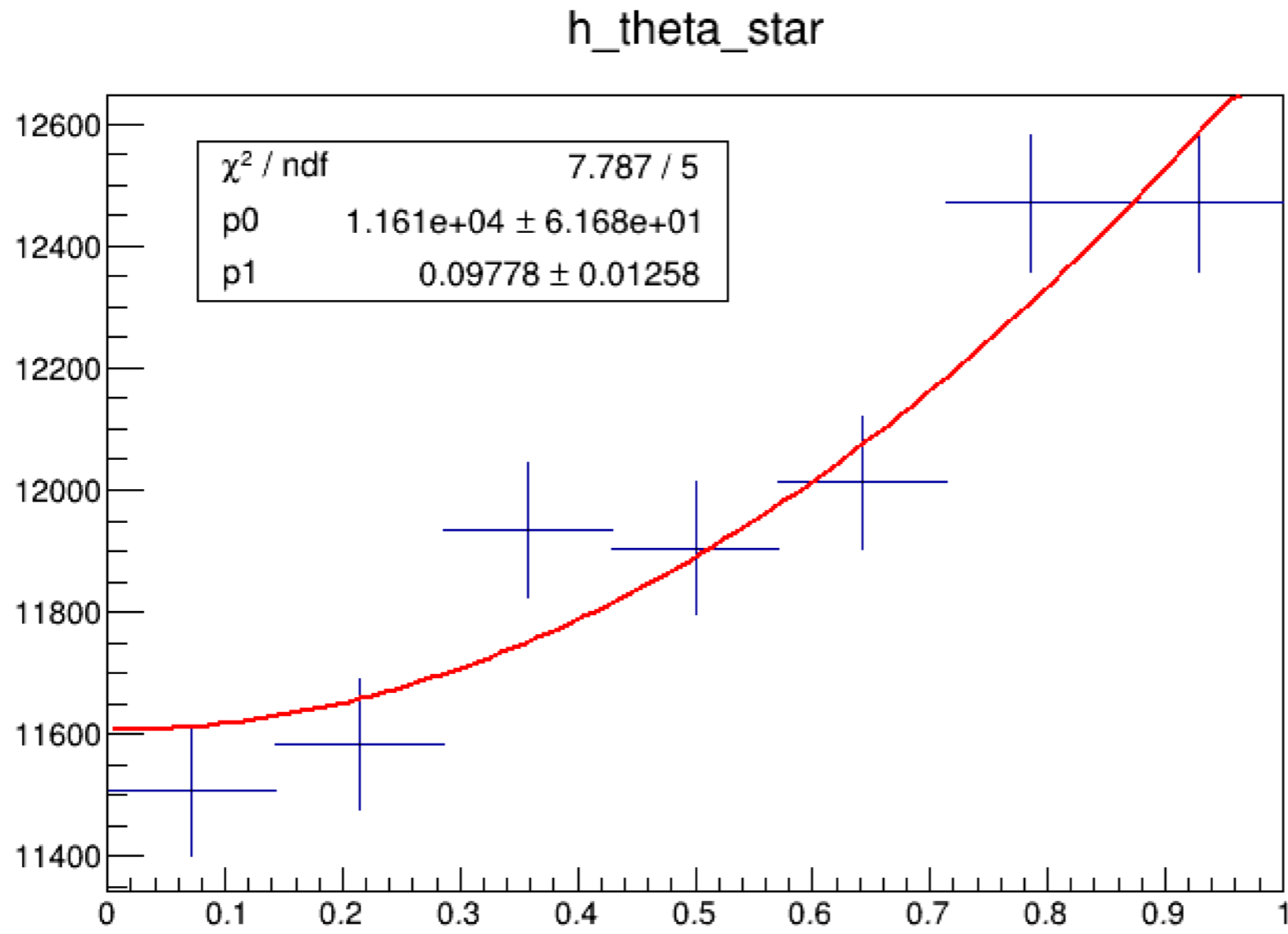
$$|\eta| < 0.8$$

$$\cos 2\beta: 0.0127654 \pm 0.00206018$$



$$|\eta| < 0.6$$

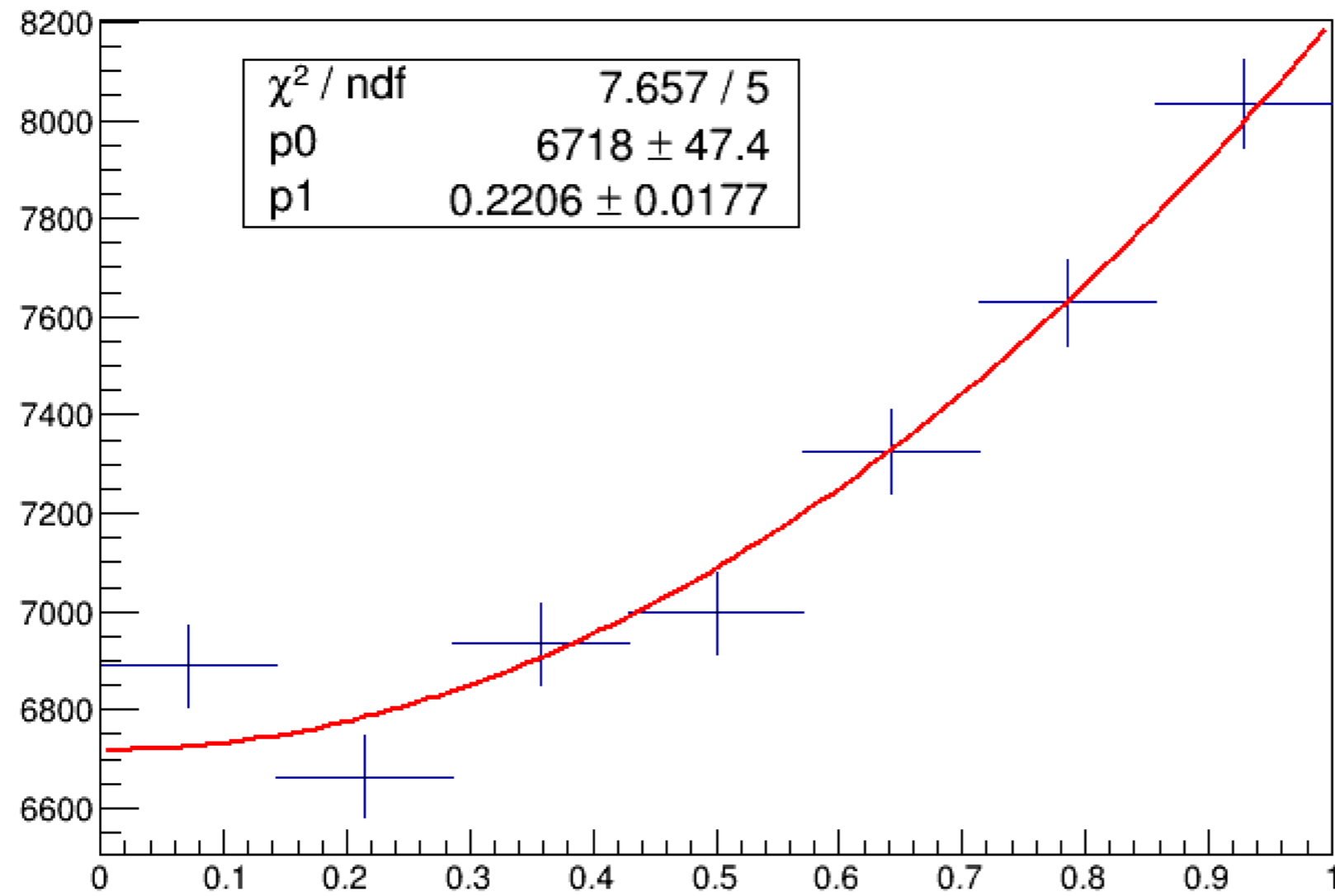
**cos2beta: 0.0273808 +/- 0.00243961**



$$|\eta| < 0.4$$

**cos2beta: 0.0721493 +/- 0.00313708**

h\_theta\_star



$$|\eta| < 0.2$$

**cos2beta: 0.251166 +/- 0.00508128**

h\_theta\_star

